

CUHK
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Games, Privacy and Distributed Inference for the Smart Grid

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Games, Privacy and Distributed Inference for the Smart Grid



Overview

Three Topics in Smart Grid:

Games, Privacy and Distributed Inference for the Smart Grid



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Three Topics in Smart Grid:

- *Game Theoretic Methods* for Modeling Interactions

Games, Privacy and Distributed Inference for the Smart Grid



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- *Privacy-Utility Tradeoffs* for Data Sources

Games, Privacy and Distributed Inference for the Smart Grid



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- *Game Theoretic Methods* for Modeling Interactions
- *Privacy-Utility Tradeoffs* for Data Sources
- *Distributed Algorithms* for State Estimation

Games, Privacy and Distributed Inference for the Smart Grid



Game Theoretic Methods for Modeling Interactions

Joint work with Walid Saad, et al.

Games, Privacy and Distributed Inference for the Smart Grid



Introduction & Motivation

- Salient characteristics of smart grid:
 - **Heterogeneity:** in terms of node types (electric vehicles, smart meters, substations, etc.) with each node having its own objective.
 - **Large-scale interactions:** spans large geographical areas and could incorporate thousands if not millions of nodes.
 - **Stochastic dynamics:** time-varying features, in terms of demand, supply, node dynamics (e.g., car mobility), etc.

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 - **Non-cooperative** game theory
 - **Cooperative** game theory

Game Theoretic Methods for Modeling Interactions



Introduction & Motivation

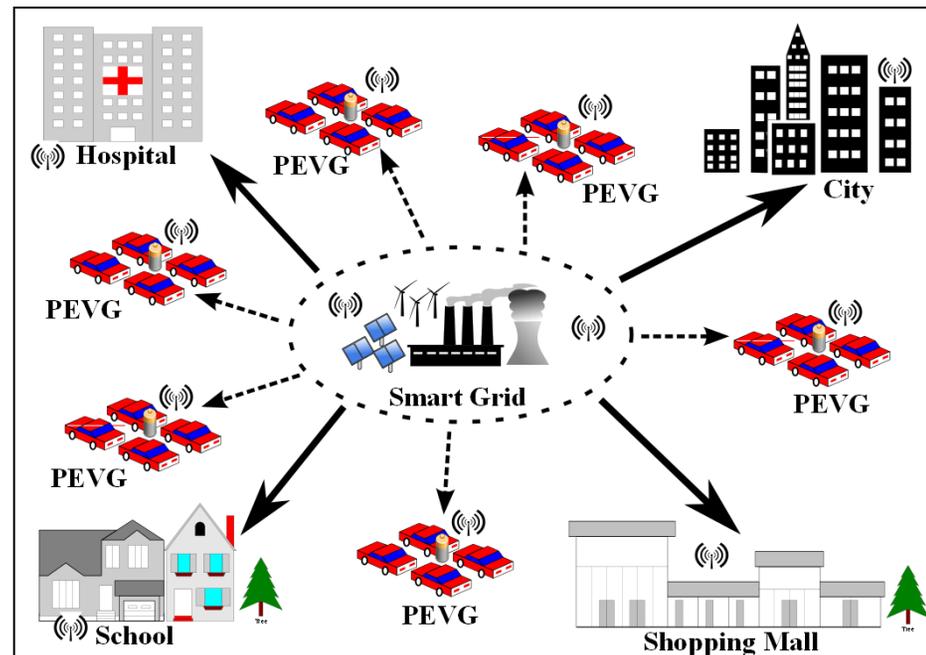
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- Illustrate via **two examples**

Game Theoretic Methods for Modeling Interactions



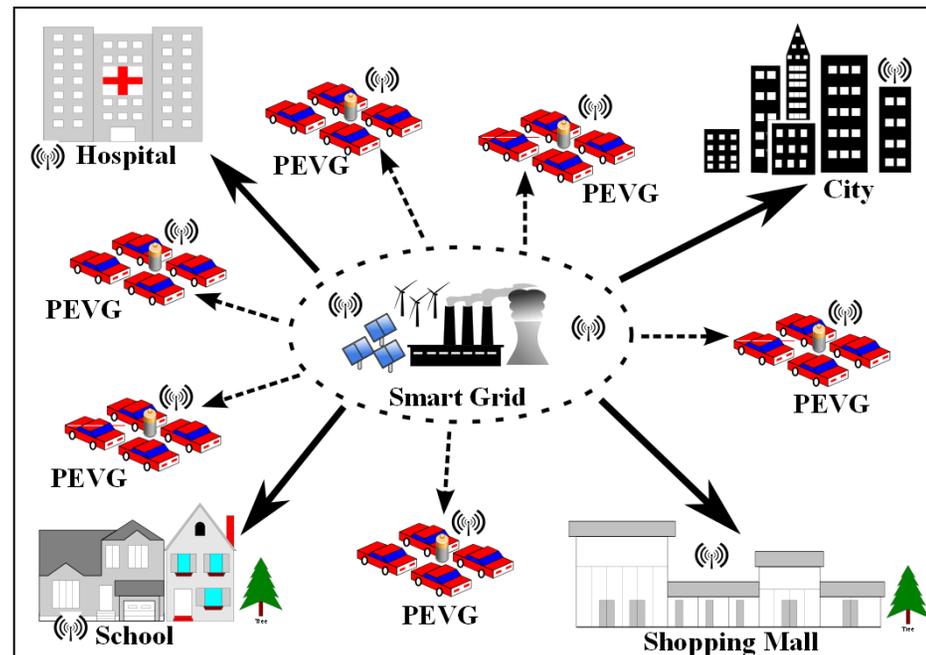
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- Groups of **plug-in electric vehicles** can trade energy with the main grid.



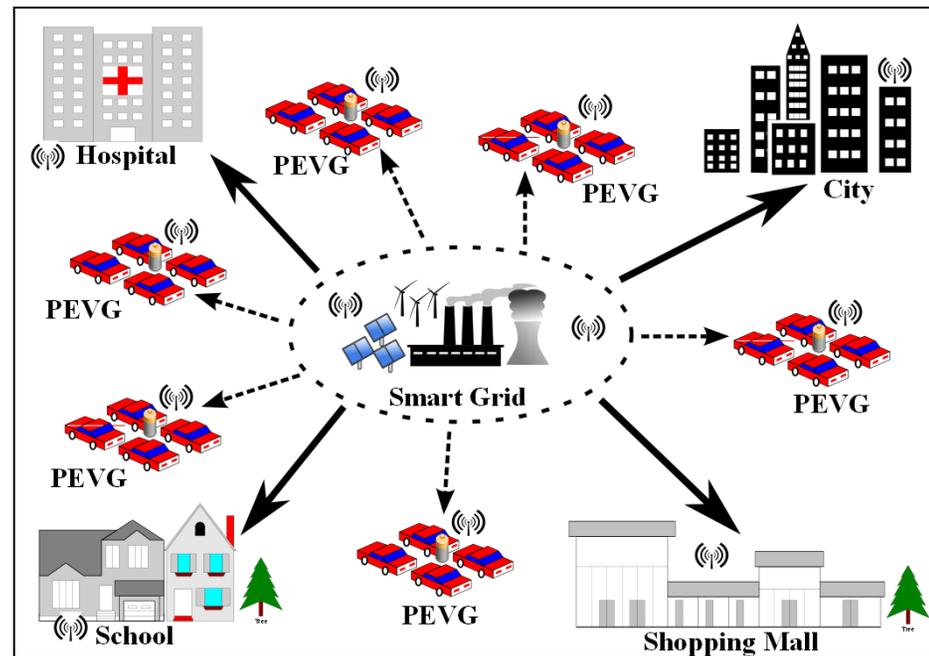
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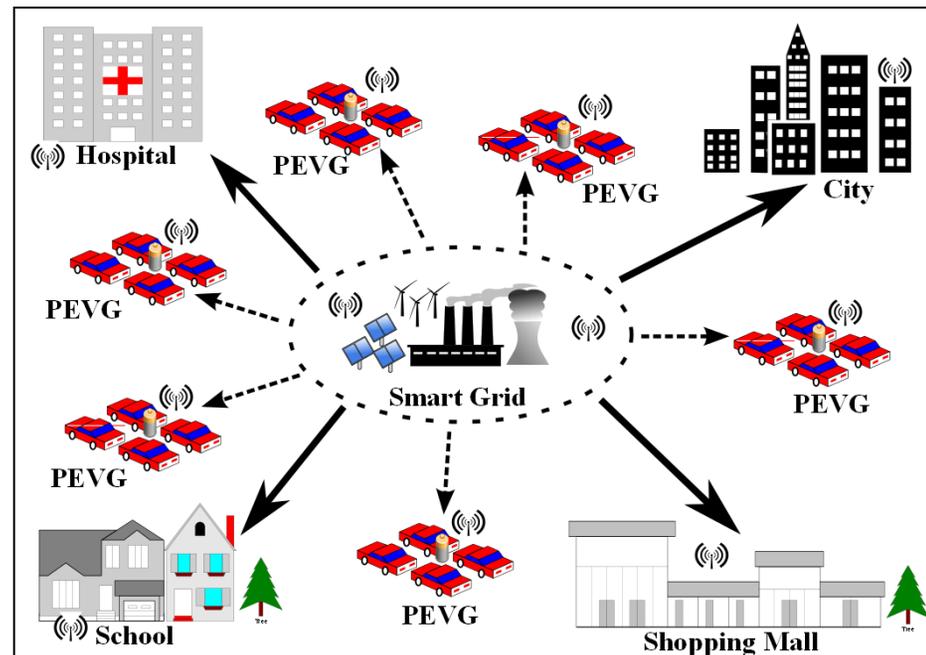
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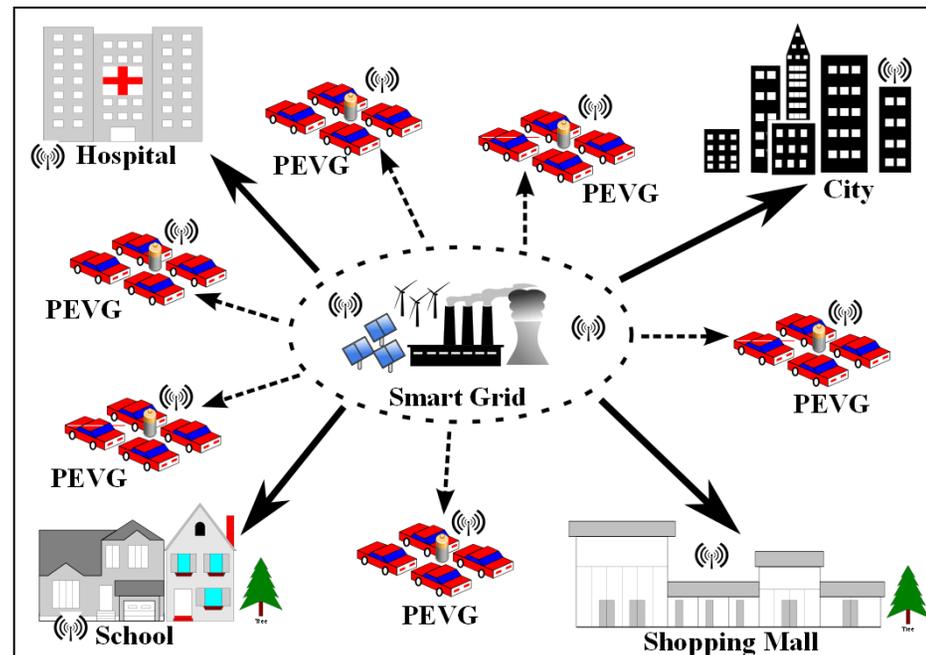
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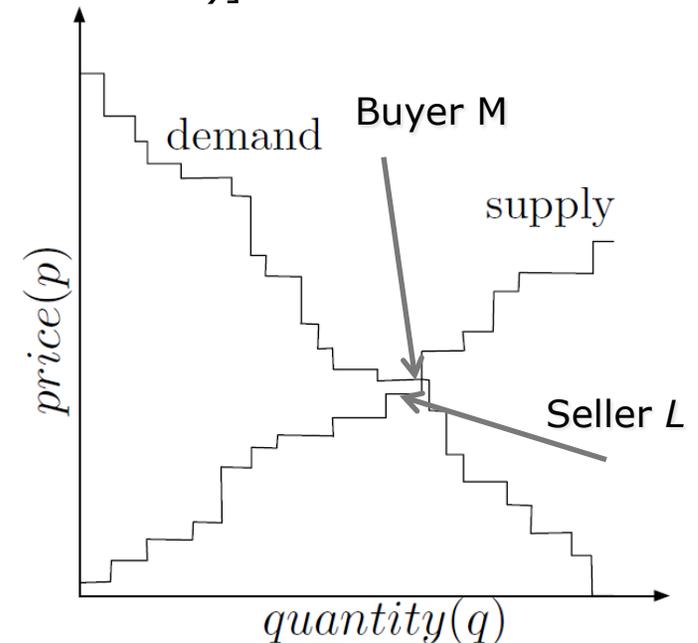
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- If grid elements act autonomously, a hybrid **auction/Nash game** can be used. Consider this first, with the EV groups **selling** ...



Double Auction Market Model

[w/ Saad, Han, Basar – T-SG (submitted)]

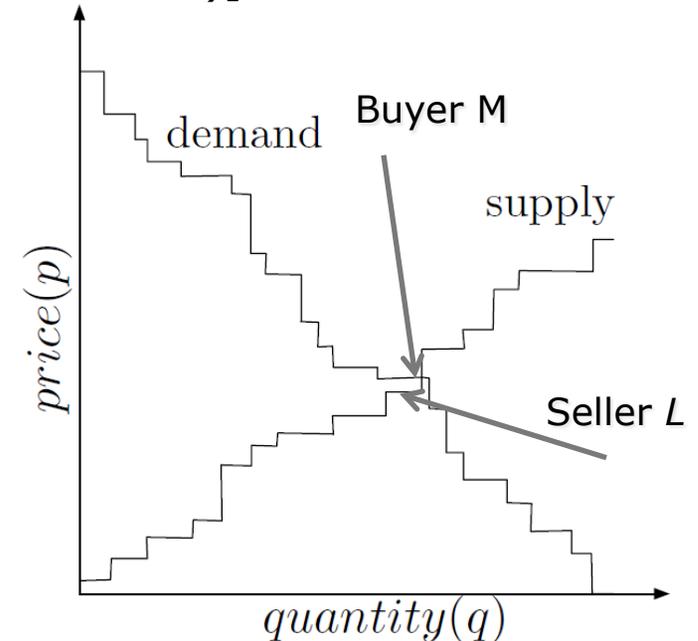
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 - Order buyers by decreasing bids and sellers by increasing prices
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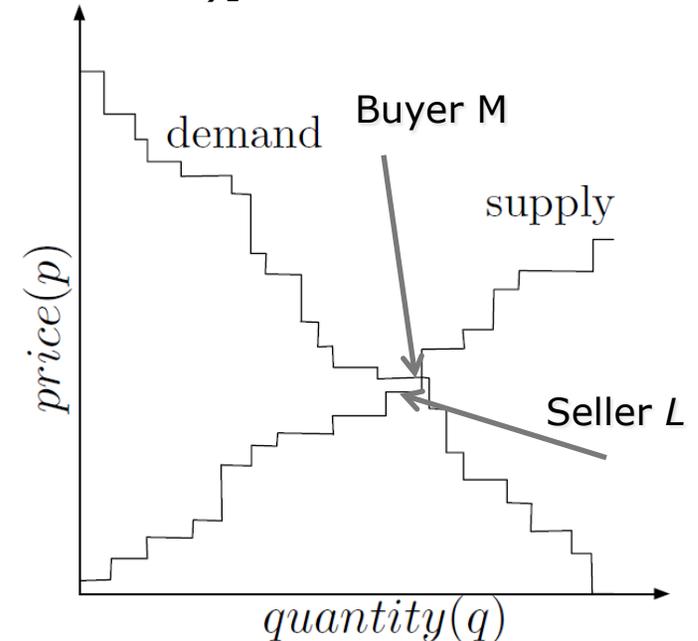
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- The number and identity of the sellers and buyers that will trade; assume $L-1$ sellers and $M-1$ buyers trade
- The trading price is given by

$$\bar{p}(\mathbf{a}) = \frac{s_L + b_M}{2}$$

\mathbf{a} is the vector of energy put up for sale, s_L and b_M are the reservation bids of seller L and buyer M



Game Theoretic Methods for Modeling Interactions



A Non-Cooperative Game

[w/ Saad, Han, Basar – T-SG (submitted)]

- The **strategy** of a vehicle group i is to choose the **maximum** amount a_i of **energy to sell**.



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- Vehicle group i chooses its strategy to **maximize its utility**:

$$U_i(a_i, \mathbf{a}_{-i}) = (\bar{p}(\mathbf{a}) - s_i)Q_i(\mathbf{a}) - \tau_i Q_i^2(\mathbf{a})$$

Trading price
(auction outcome)

Quantity sold
(auction outcome)

Pricing factor

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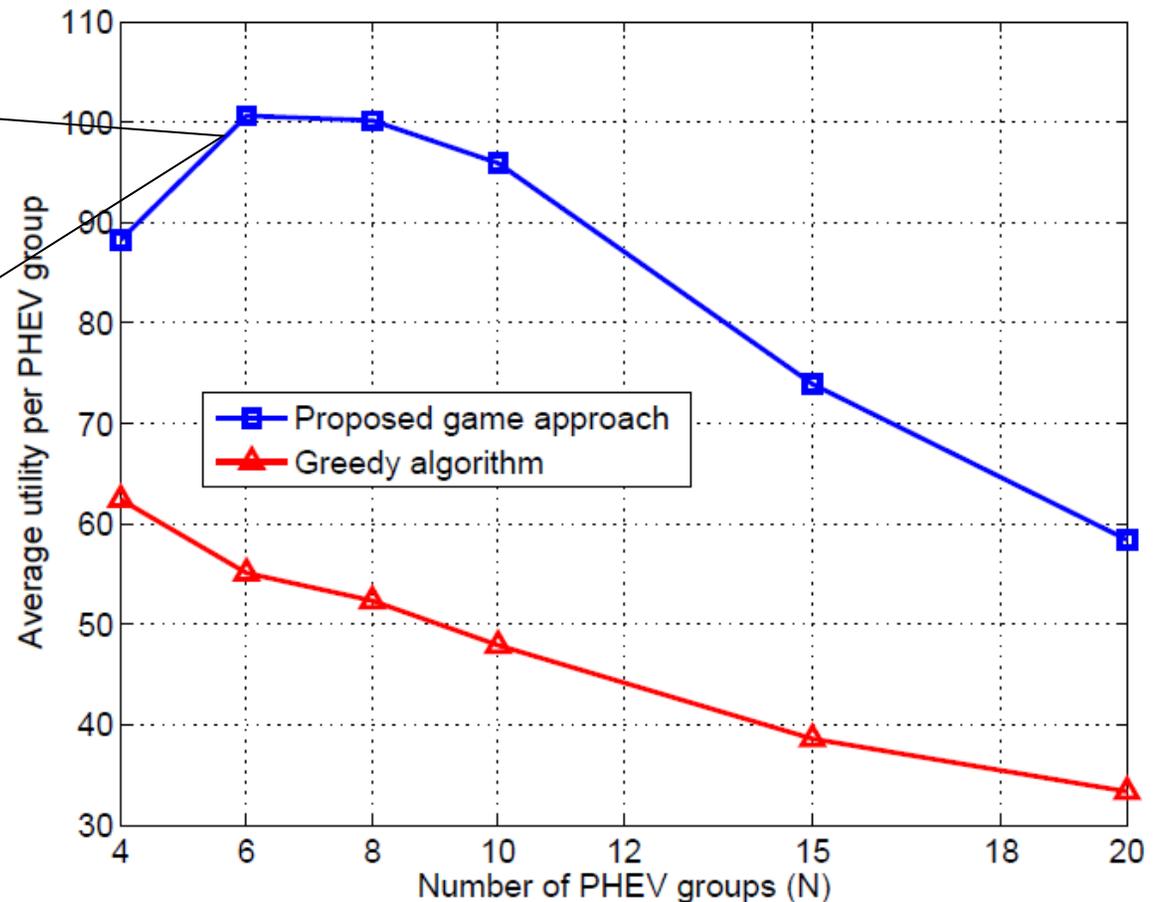
- How to solve the game and find the **Nash equilibrium**?
 - Auction introduces a discontinuity => difficult analytically
 - Algorithmic approach (based on **best-response**)

Game Theoretic Methods for Modeling Interactions



Typical Simulation Results

- Initially, the utility increases as **more players enter** the game leading to **more energy sold**.
- Then, the utility decreases as the presence of **more sellers deflates the price**.



A Stackelberg Model

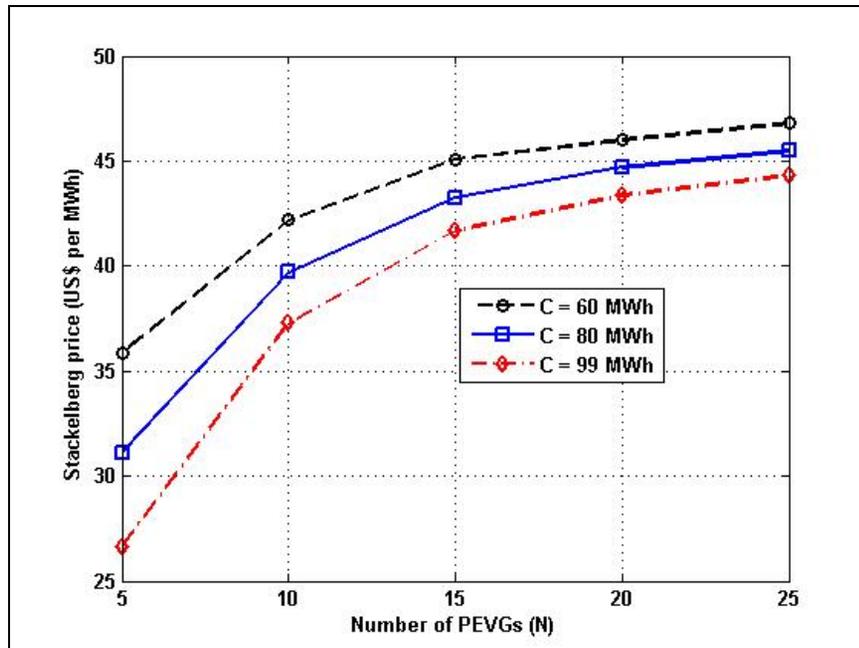
[w/ Tushar, Saad, Smith - T-SG'12]

- Consider now the grid acting as a **single** entity (and selling to the vehicle groups).
- Then we have a powerful **leader** (the grid) and less powerful (and competing) **followers** (the vehicle groups) - a Stackelberg game
- The utilities of the vehicle groups are still **linear-quadratic** in their strategies (i.e., how much they buy).
- But, the **price is set by the leader**.
- The leader's utility is bi-linear = **price** × **total quantity sold**.
- Leads to a **Stackelberg equilibrium**.

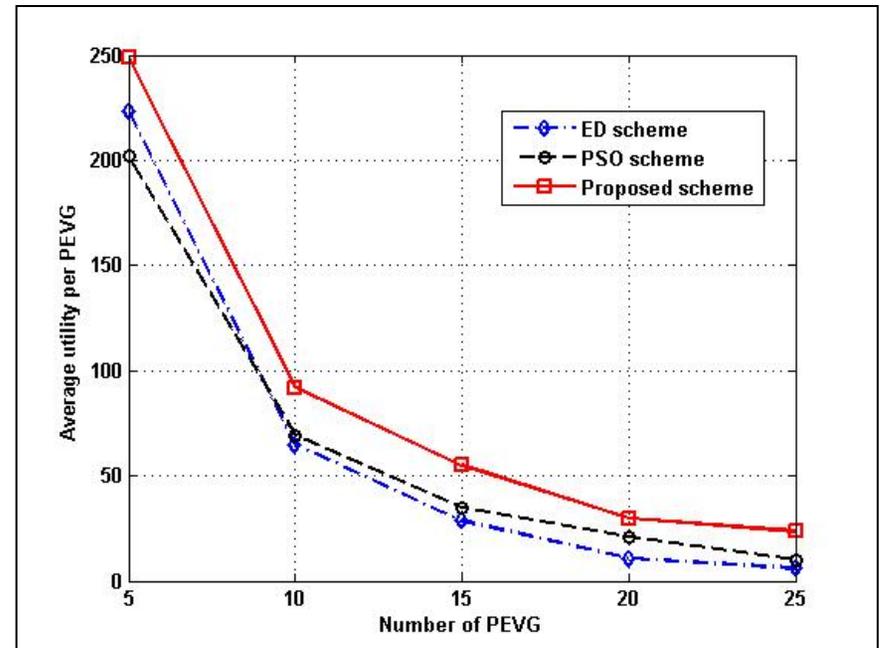
Game Theoretic Methods for Modeling Interactions



Typical Simulation Results



Price vs. # Groups



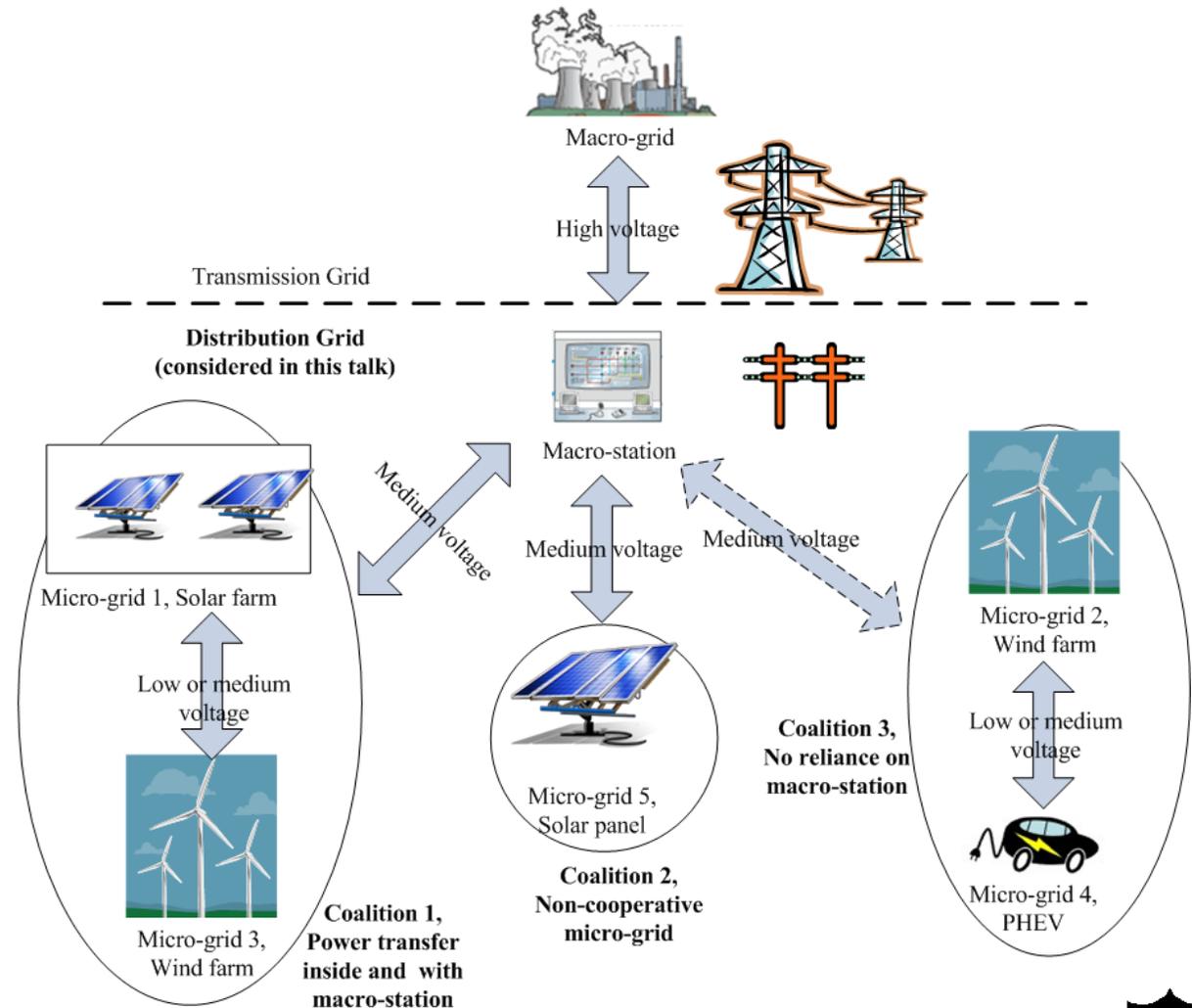
Ave. Utility vs. # Groups*

*PSO = particle swarm optimization
ED = equal distributions

Ex. 2: Micro-grid Interaction

[w/ Saad, Han – ICC'11]

- Energy trading within the distribution network



Game Theoretic Methods for Modeling Interactions



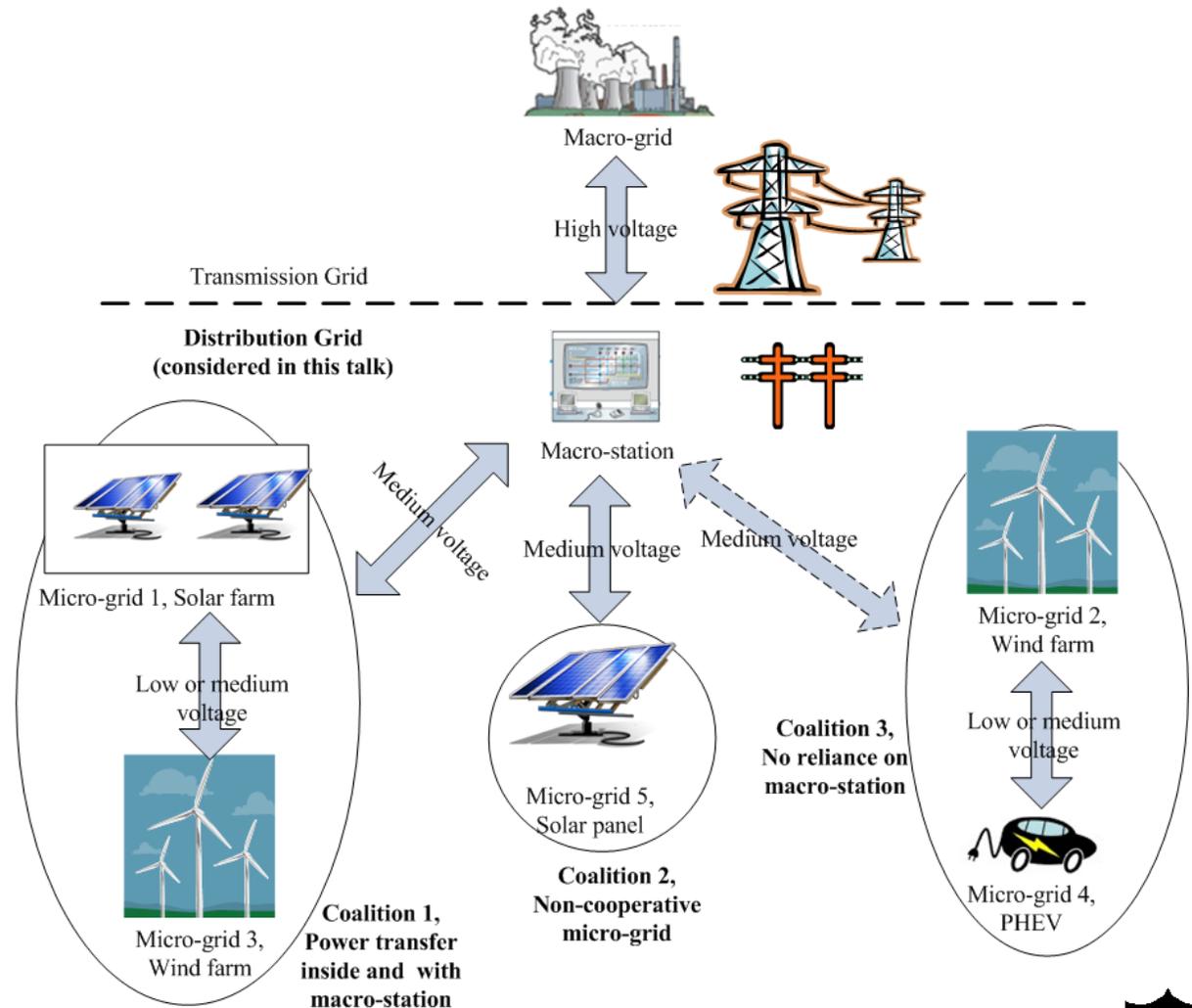
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- Cooperation helps to:

- Exchange energy: sell surplus and overcome deficiency
- Reduce power losses over transmission lines



Game Theoretic Methods for Modeling Interactions



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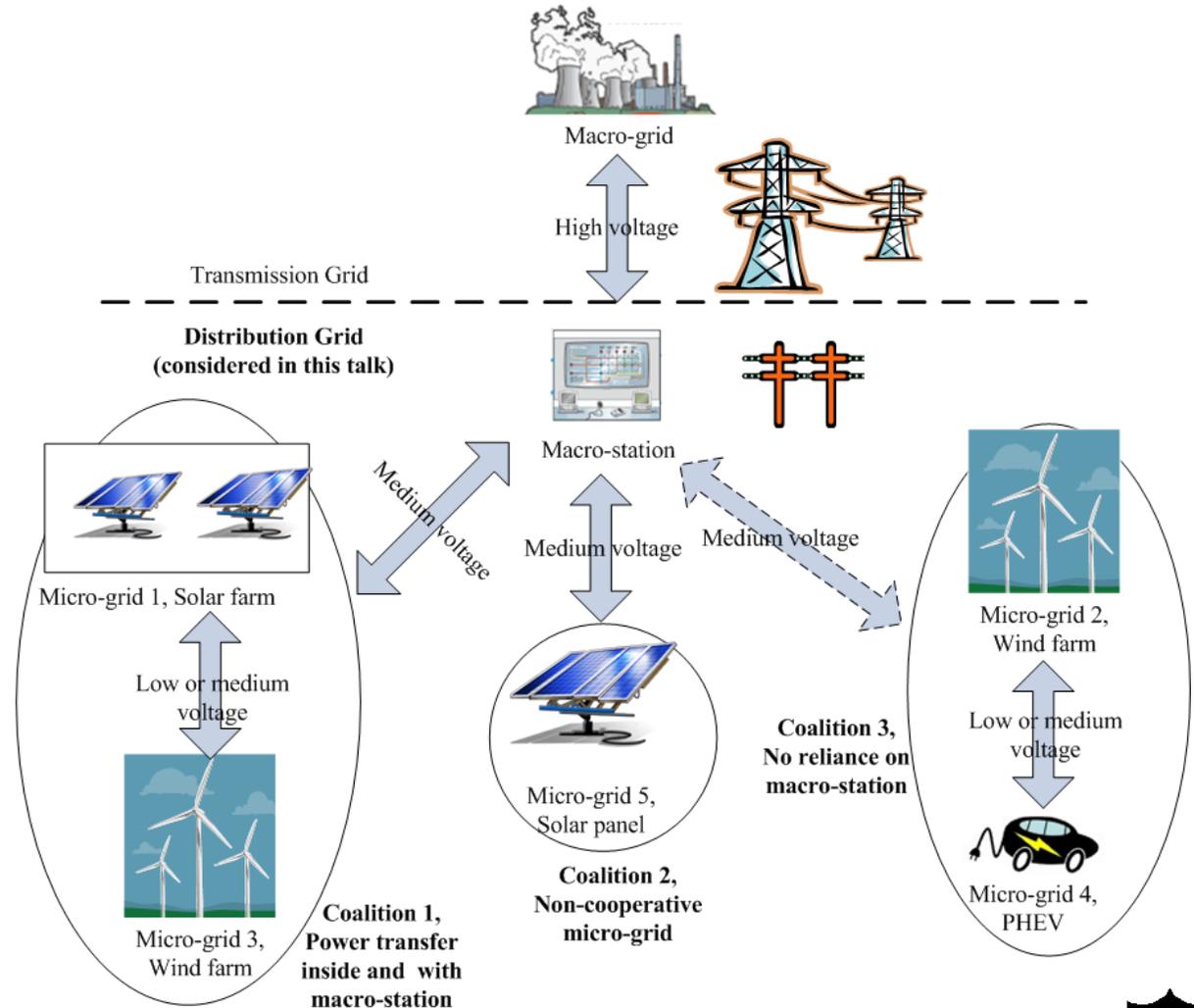
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- Coalitional games



Game Theoretic Methods for Modeling Interactions



Coalition Games

- Coalitional game (N, v)
 - In a set of players N , a *coalition* S is a **group of cooperating players**
 - **Value** (utility) of a coalition $v(S)$
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- Coalition formation
 - Coalitions can be compared based on **Pareto ordering** of user payoffs
 - **Merges and splits** can be used to iterate on coalitions
 - Convergence to a stable, **merge-and-split-proof limit**



Game Formulation: Value Function

- For a coalition S , we define the value function as

$$v(S) = \max_{\pi \in \mathcal{I}_S} u(S, \pi)$$

- The max is **over all orderings** of buyers & u measures **power losses**.
- The utility represents a **cost paid** per unit of **power loss**.



Game Formulation: Value Function

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- To divide the utility between the players, adopt a **fair division proportional** to the **non-cooperative utility** of each user:

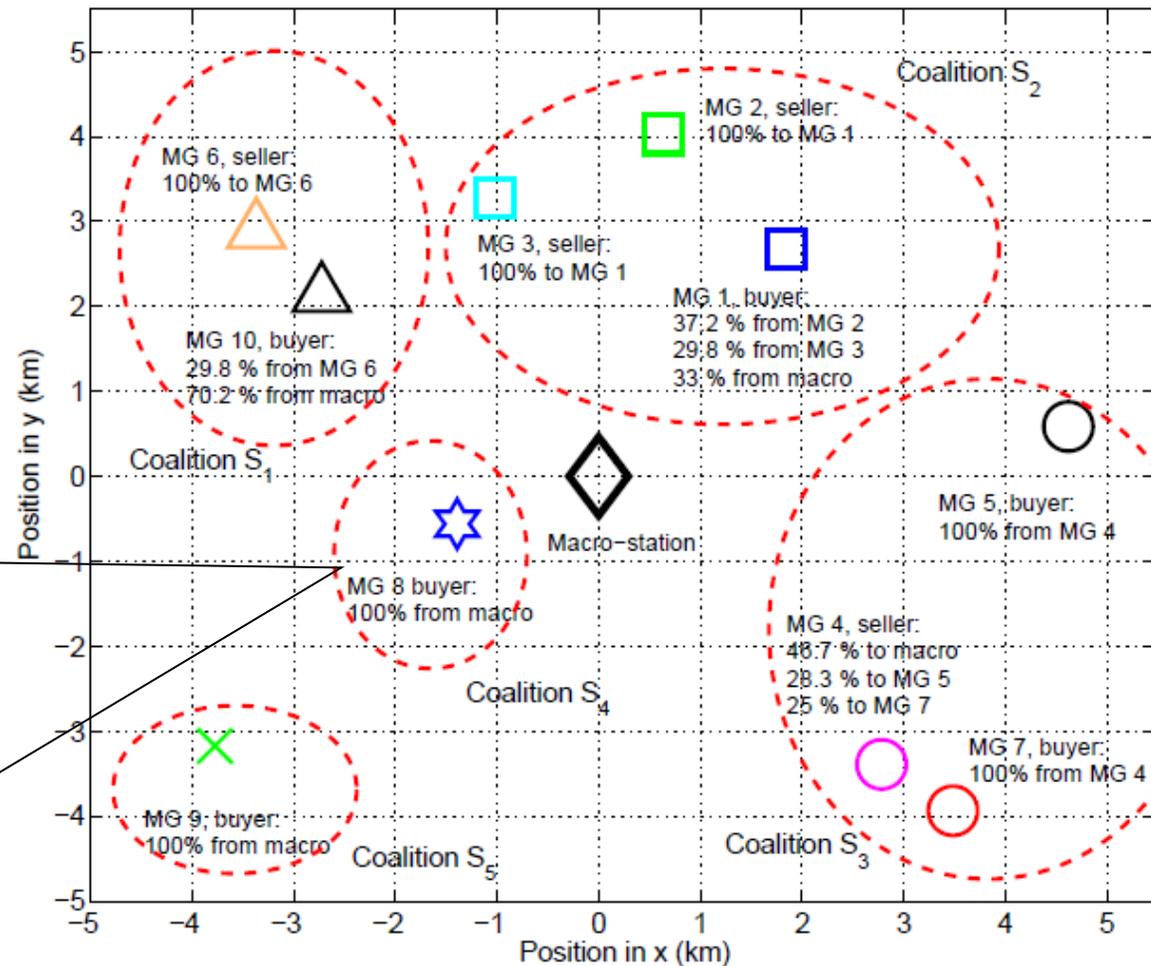
$$\phi_i = \alpha_i \left(v(S) - \sum_{j \in S} v(\{j\}) \right) + v(\{i\}).$$

Weight chosen according to micro-grid i 's **non-cooperative utility**

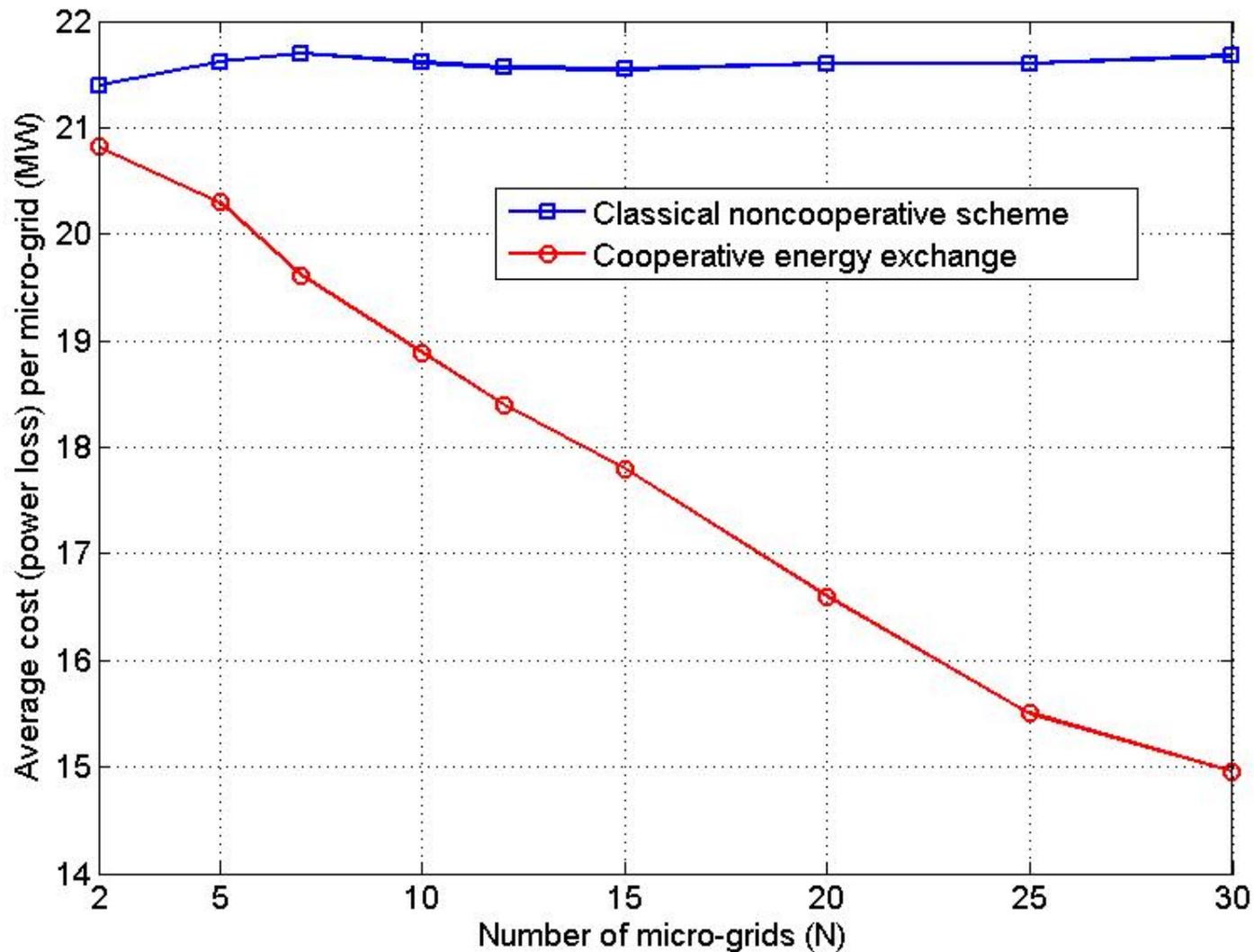
$$\frac{\alpha_i}{\alpha_j} = \frac{v(\{i\})}{v(\{j\})} \quad \sum_{i \in S} \alpha_i = 1$$

Typical Simulation Results (1)

- Emergence of **local markets**
- Here, we see a **single snapshot**; it is of interest for future work to see how this evolves as demand/supply vary



Typical Simulation Results (2)



Game Theoretic Methods for Modeling Interactions



Summary

- Game theory for **smart grid modeling**:
 - **Demand-side management**, energy trading and markets
 - Integration and distributed **operation of micro-grids**
 - “Game theoretic methods for the smart grid,” [w/ Saad, Han, Basar - **SPM'12**]

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- Other problems of interest
 - **Network formation games** for PLC backhaul [w/ Saad, Han - **Gamenets'11**]
 - **Social optimality** of equilibria in trading markets [w/ Tushar, et al. - **ICC'13**]

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- Additional issues
 - Optimizing jointly over **three layers**: economic, cyber, and physical
 - Incorporating **dynamics** (generation/load/mobility/etc.)

Game Theoretic Methods for Modeling Interactions



Privacy-Utility Tradeoffs for Data Sources

Joint work with Lalitha Sankar, et al.

Games, Privacy and Distributed Inference for the Smart Grid



Motivation: The Privacy Problem

- There are many **electronic information sources** of information about us.
 - Google, Facebook, smart metering, etc.



Privacy-Utility Tradeoffs for Data Sources



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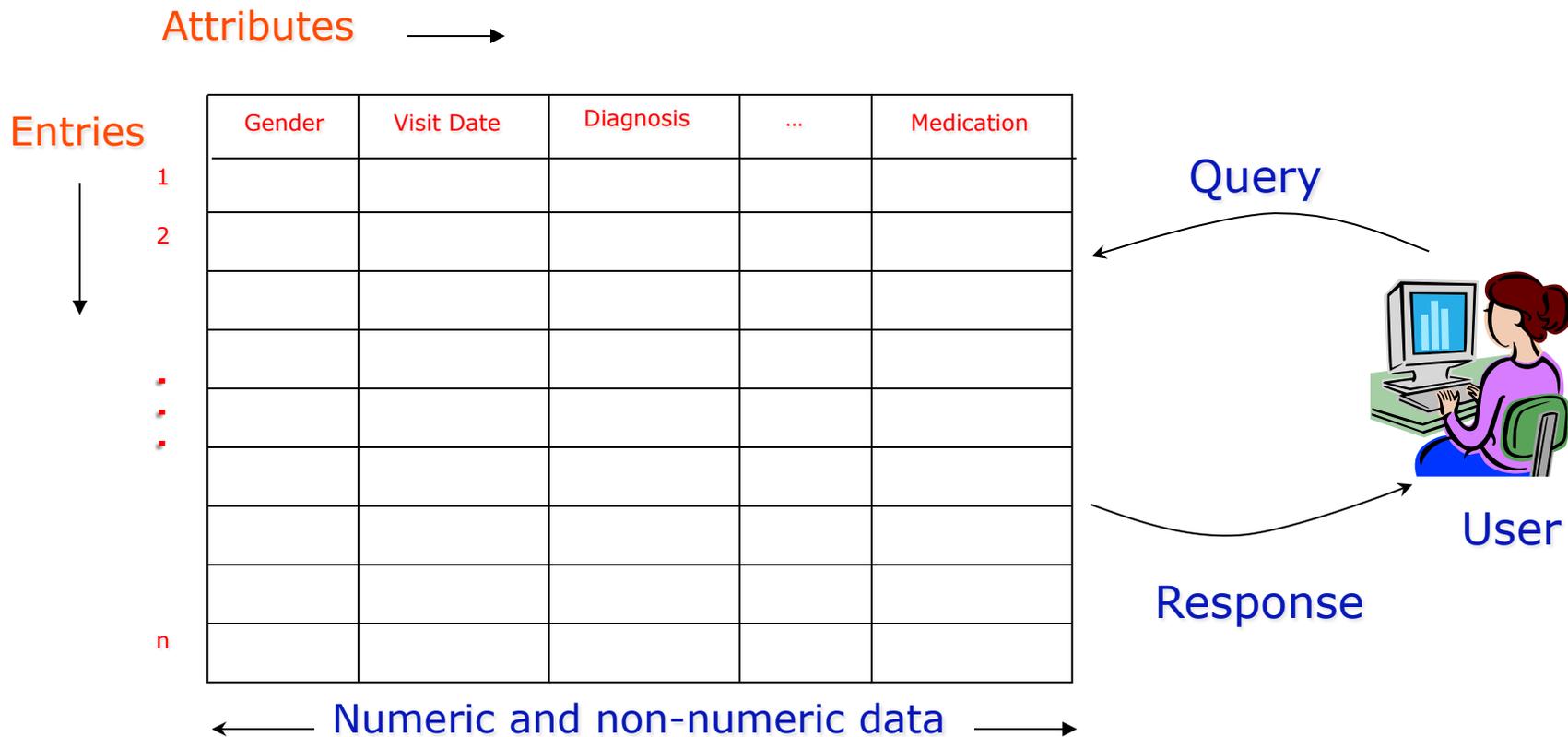
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- But, they can also **leak private information**.
- How can we **characterize this fundamental tradeoff?**

Privacy-Utility Tradeoffs for Data Sources



Database Model

A database is a **table** – rows: individual entries (total of n);
columns: attributes for each individual (total of K)



Privacy-Utility Tradeoffs for Data Sources



Database: Source Model

- Database with n rows is a sequence of n i.i.d. observations of a vector random variable $\mathbf{X} = (X_1 X_2 \dots X_K)$ with a joint distribution:

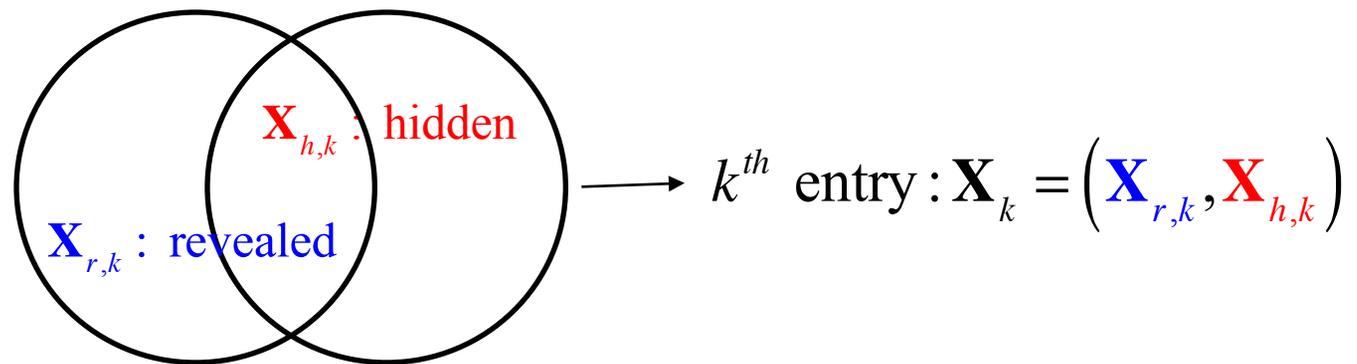
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- Attributes divided into **public** (revealed) and **private** (hidden) variables, typically not disjoint:



Privacy-Utility Tradeoffs for Data Sources



Privacy-Utility Tradeoff

[w/ Sankar, Rajagapolan - T-IFS'13]

- Contrast between privacy and secrecy:

Privacy-Utility Tradeoffs for Data Sources



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 - Measure **privacy** by **equivocation** on the **private variables** in information revealed to a user.
- Then the **distortion-equivocation** region describes the tradeoff.

Privacy-Utility Tradeoffs for Data Sources



Distortion-Equivocation Model

[w/ Sankar, Rajagapolan - T-IFS'13]

- Encoder maps the original database to a “sanitized” database (SDB):

$$\text{Encoder} : \mathbf{X}^n \rightarrow \mathcal{W} = \{SDB_1, SDB_2, \dots, SDB_M\}$$

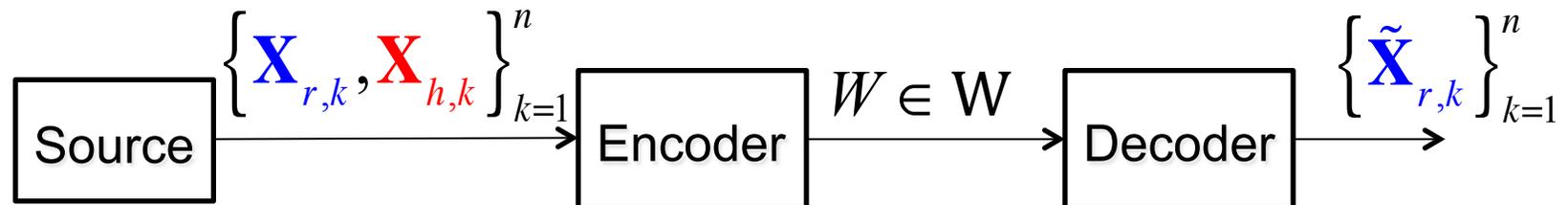


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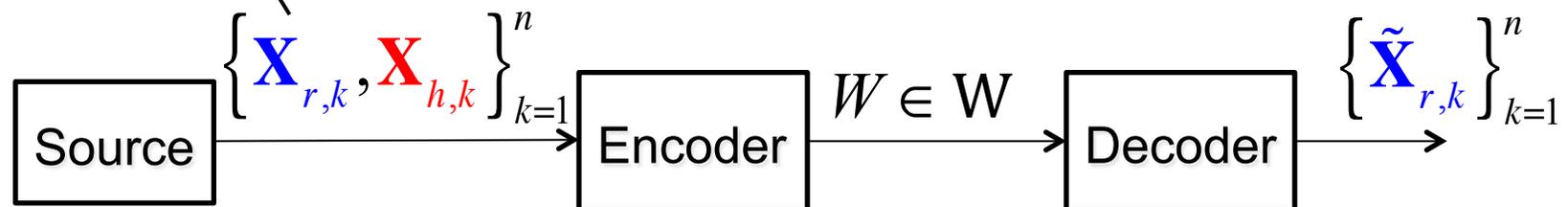
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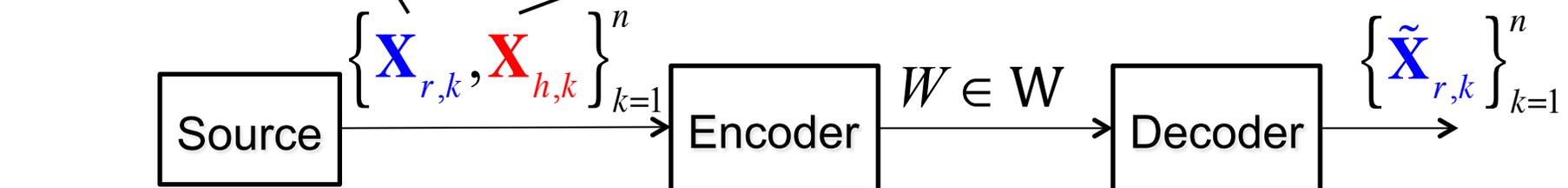
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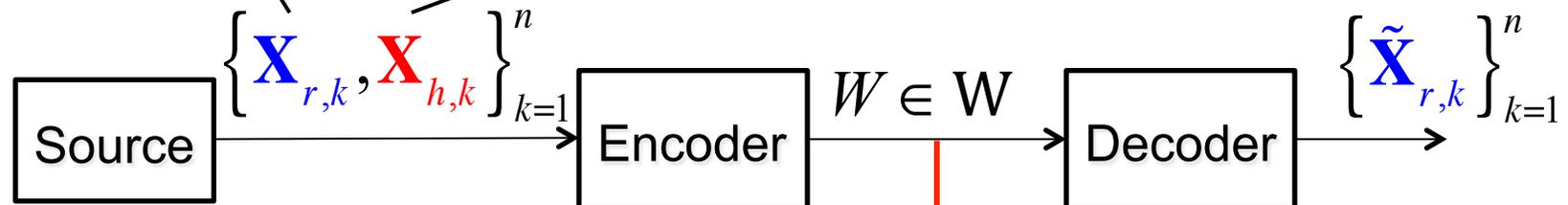
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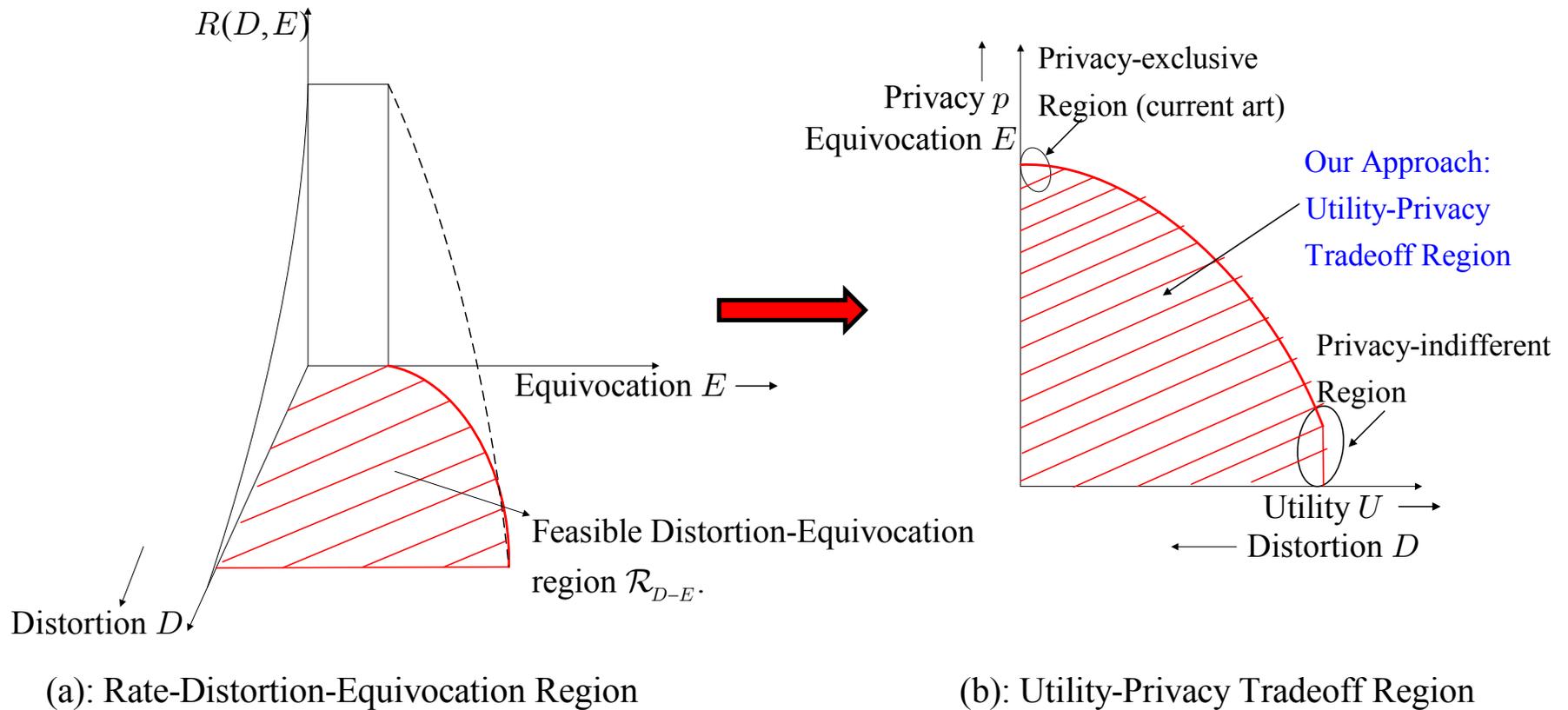
Add a rate constraint \rightarrow

$$M \leq 2^{n(R+\varepsilon)}$$

Privacy-Utility Tradeoffs for Data Sources



Utility-Privacy/RDE Regions

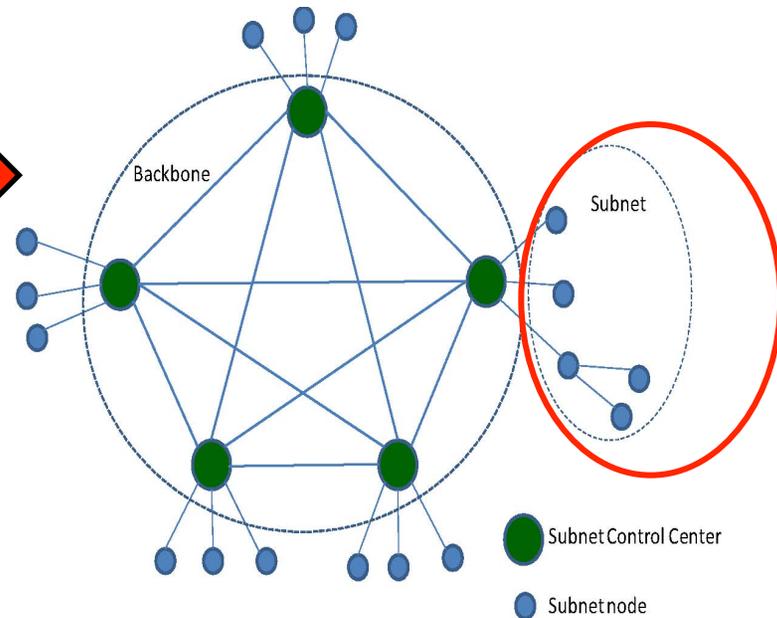
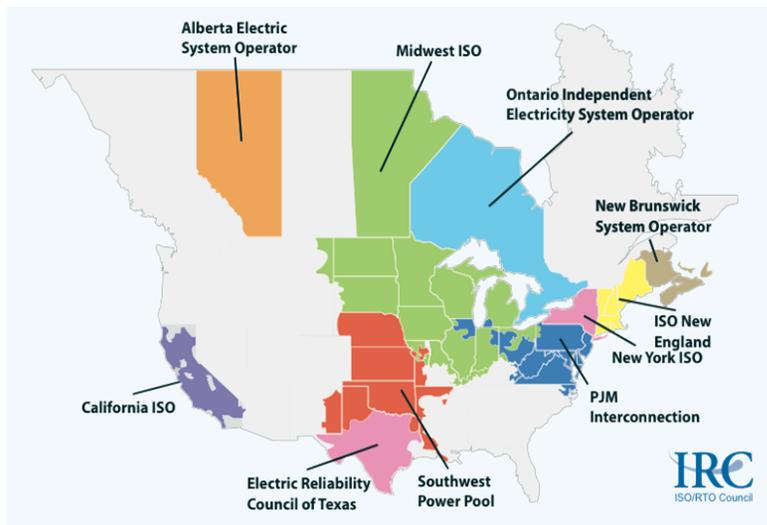


Privacy-Utility Tradeoffs for Data Sources



Competitive Privacy

- N.A. Grid: interconnected regional transmission organizations (RTOs) which
 - need to share measurements on state estimation for **reliability** (utility)

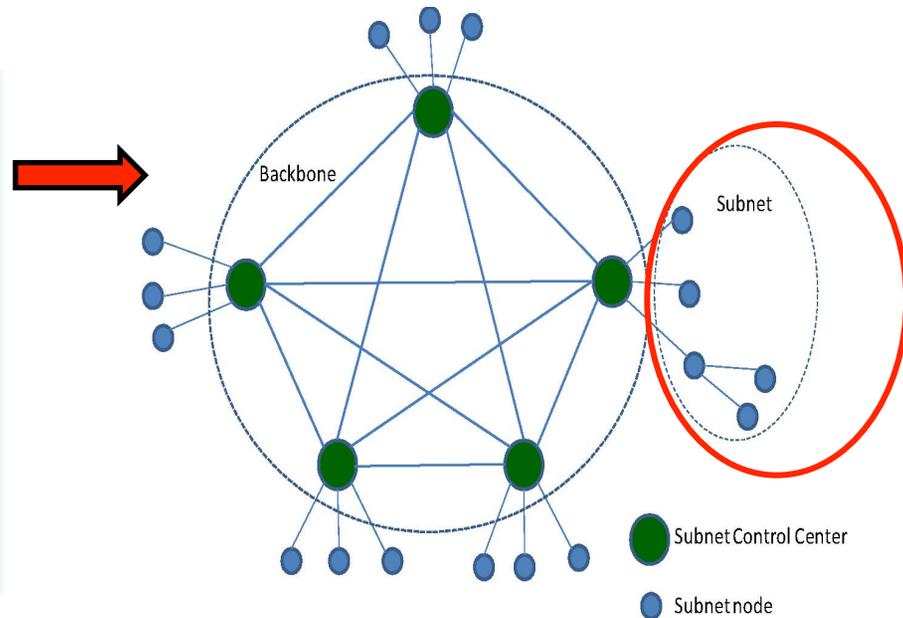
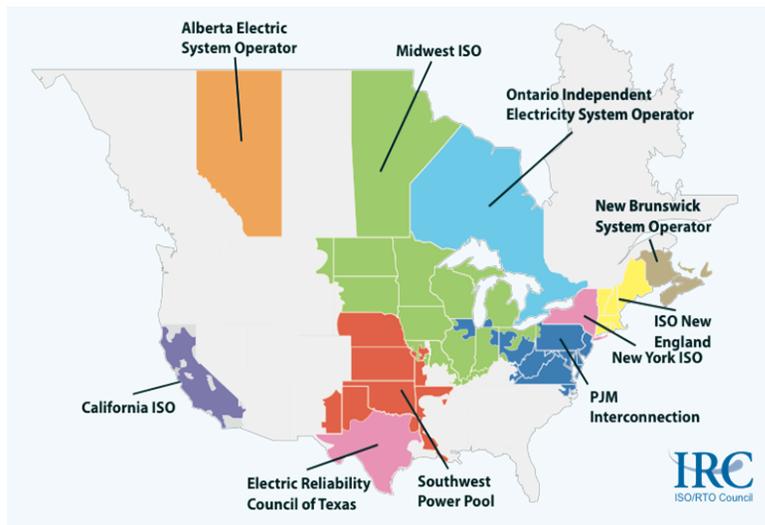


Privacy-Utility Tradeoffs for Data Sources



Competitive Privacy

- N.A. Grid: interconnected regional transmission organizations (RTOs) which
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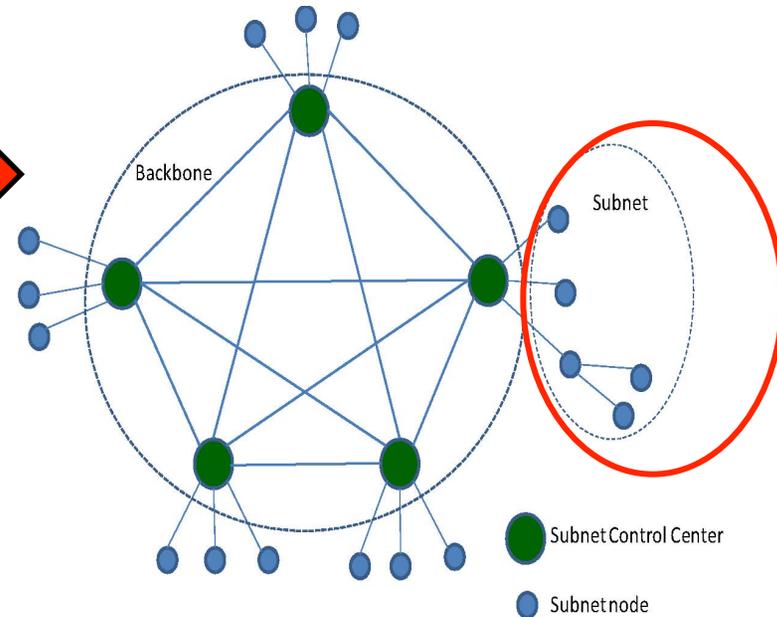
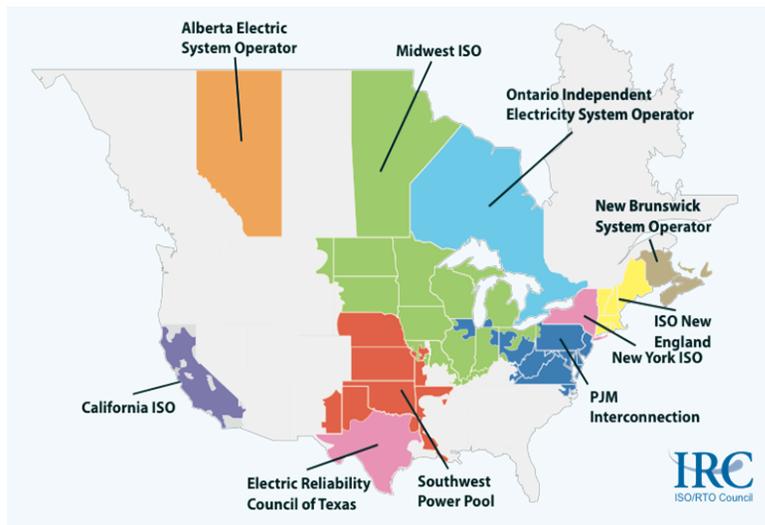


Privacy-Utility Tradeoffs for Data Sources



Competitive Privacy

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- Leads to a problem of **competitive privacy**

Privacy-Utility Tradeoffs for Data Sources



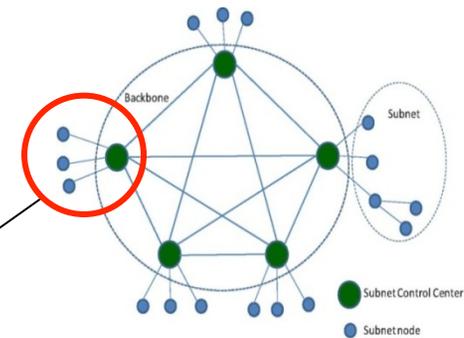
Competitive Privacy

[w / Sankar, Kar - Asilomar'12]

- Noisy measurements at RTO k :

$$Y_k = \sum_{m=1}^M H_{k,m} X_m + Z_k, \quad k = 1, 2, \dots, M$$

m^{th} system state



Privacy-Utility Tradeoffs for Data Sources



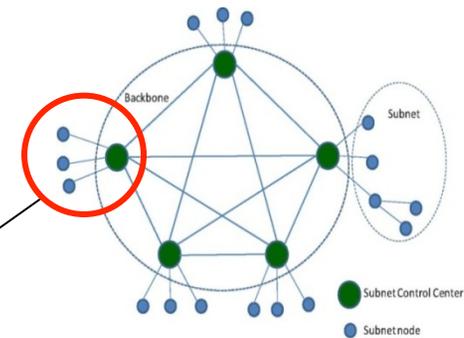
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Privacy-Utility Tradeoffs for Data Sources



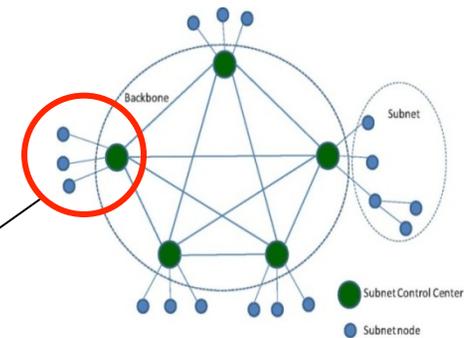
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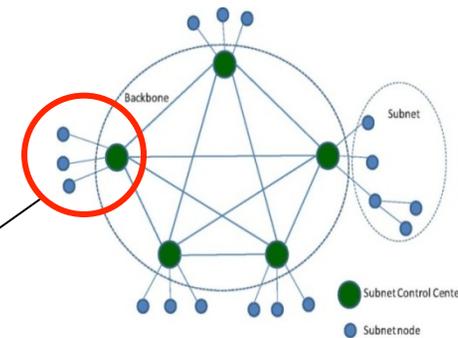
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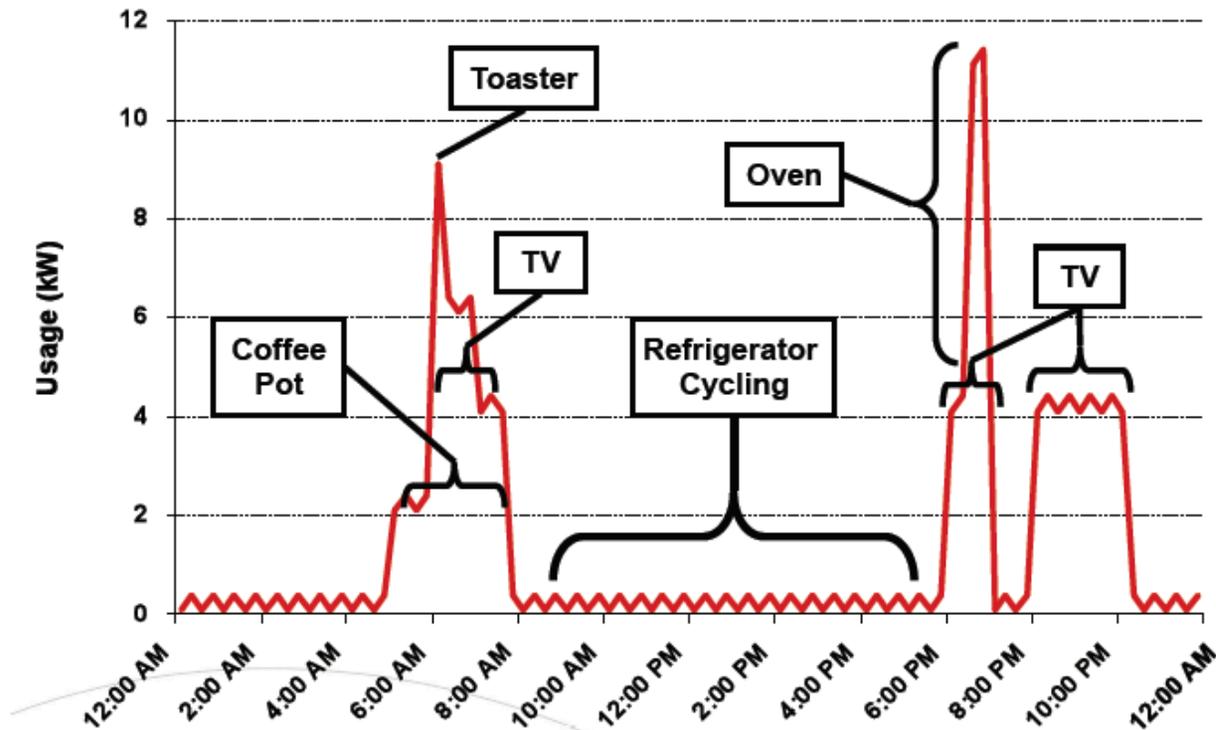
Wyner-Ziv coding **maximizes privacy for a desired utility** at each RTO.

Privacy-Utility Tradeoffs for Data Sources



Smart Meter Privacy

- Smart meter **data** is useful for **price-aware usage**, **load balancing**

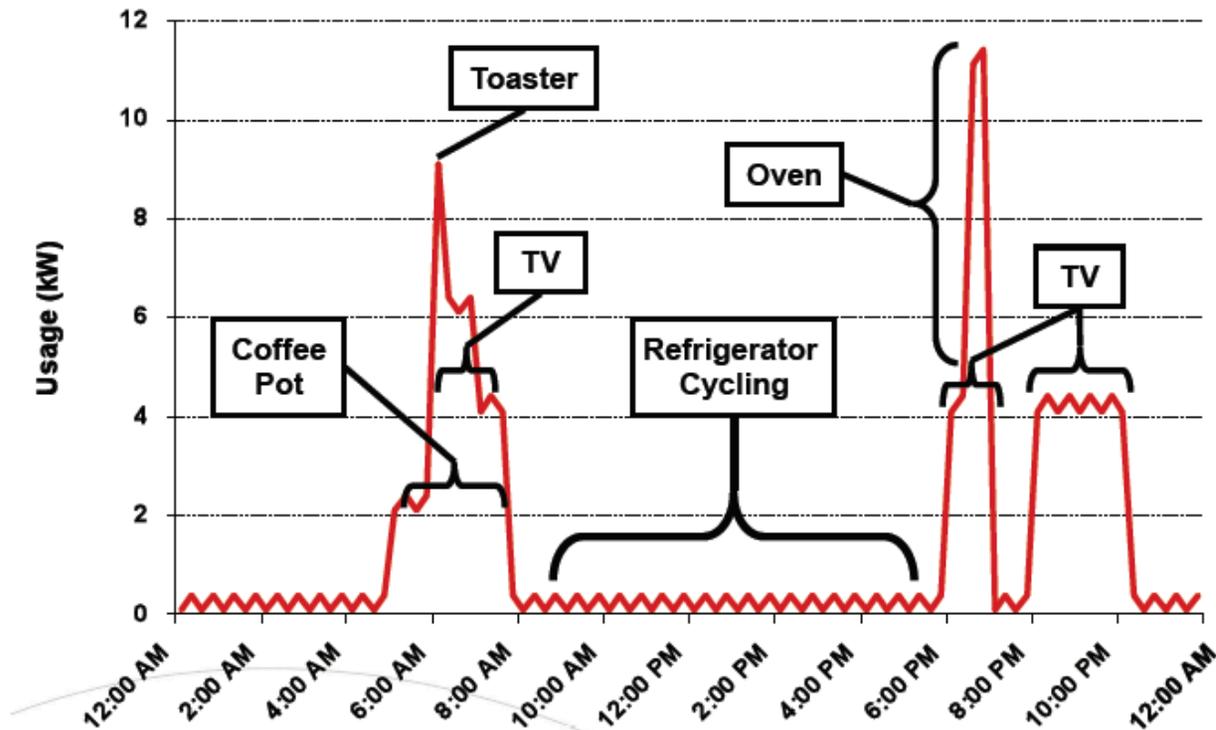


Privacy-Utility Tradeoffs for Data Sources



Smart Meter Privacy

- Smart meter **data** is useful for **price-aware usage**, **load balancing**
- But, it **leaks information** about in-home activity



Privacy-Utility Tradeoffs for Data Sources



Smart Meter Privacy

[w / Sankar, Rajagapolan, Mohajer - T-SG'13]

P-U tradeoff leads to a spectral 'reverse water-filling' solution

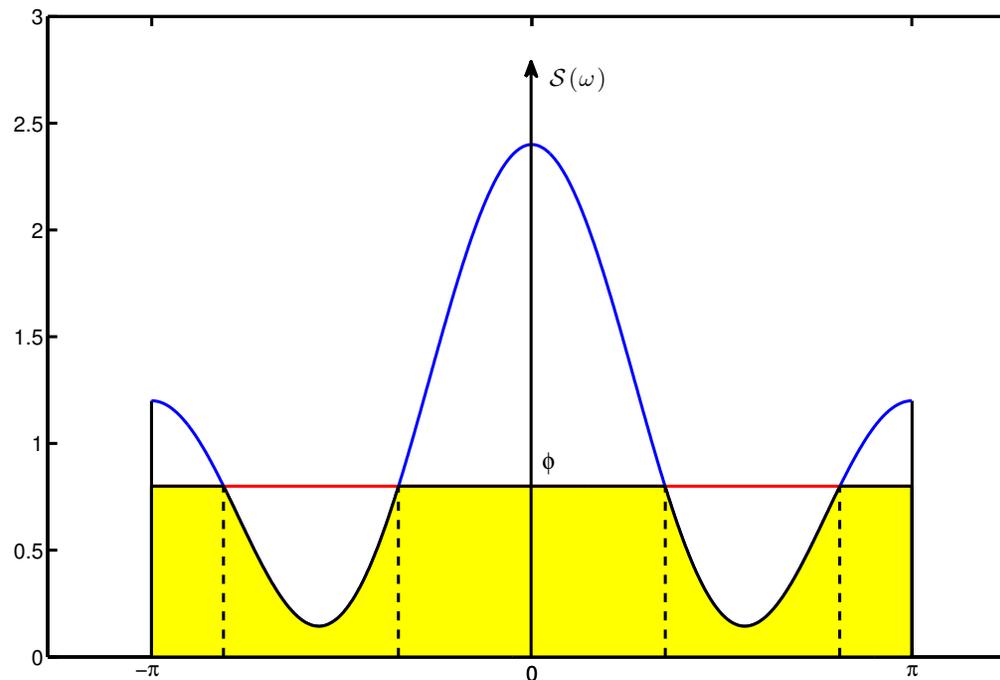
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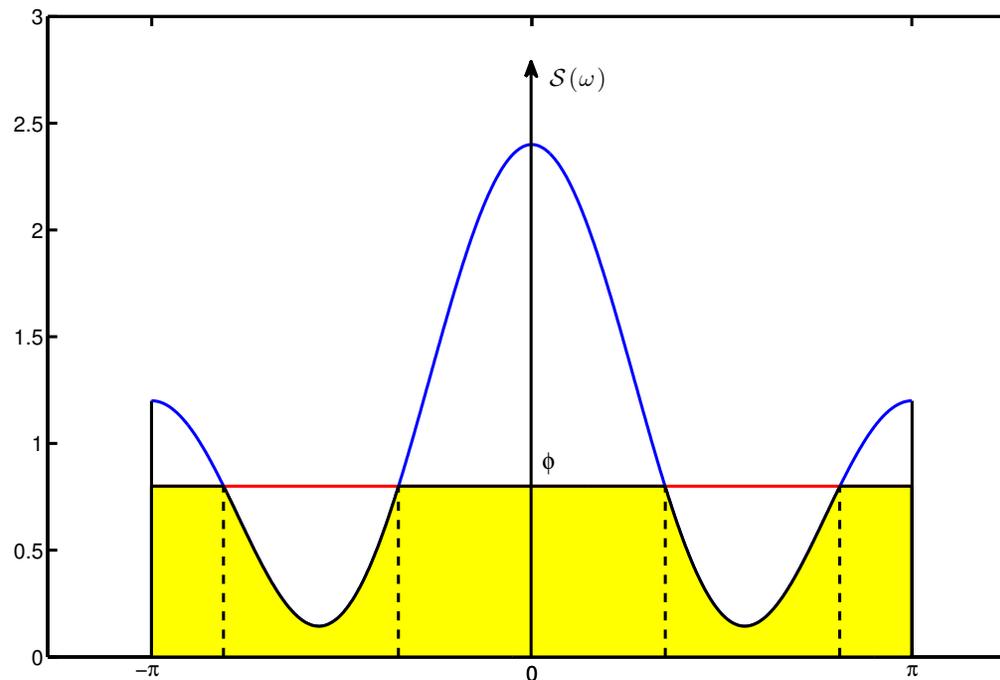
Privacy-Utility Tradeoffs for Data Sources



Smart Meter Privacy

[w / Sankar, Rajagapolan, Mohajer - T-SG'13]

P-U tradeoff leads to a spectral 'reverse water-filling' solution



Can also use energy storage to aid privacy [w/ Tan, Gunduz, JSAC:SG Series'13]

Privacy-Utility Tradeoffs for Data Sources



Summary

- An information source is divided into **private** and **public variables**
 - Leads to an **equivocation-distortion** characterization
 - Adding rate: a **rate-distortion problem** with an **equivocation constraint**



Summary

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Summary

- An information source is divided into **private** and **public variables**
 - Leads to an **equivocation-distortion** characterization
 - Adding rate: a **rate-distortion problem** with an **equivocation constraint**
- Applications in smart grid include: **competitive privacy & smart metering**
- Can also consider
 - **multiple queries** (successive disclosure)
 - **multiple sources** (side information)



Distributed Algorithms for State Estimation

Joint work with Le Xie, et al.

Games, Privacy and Distributed Inference for the Smart Grid



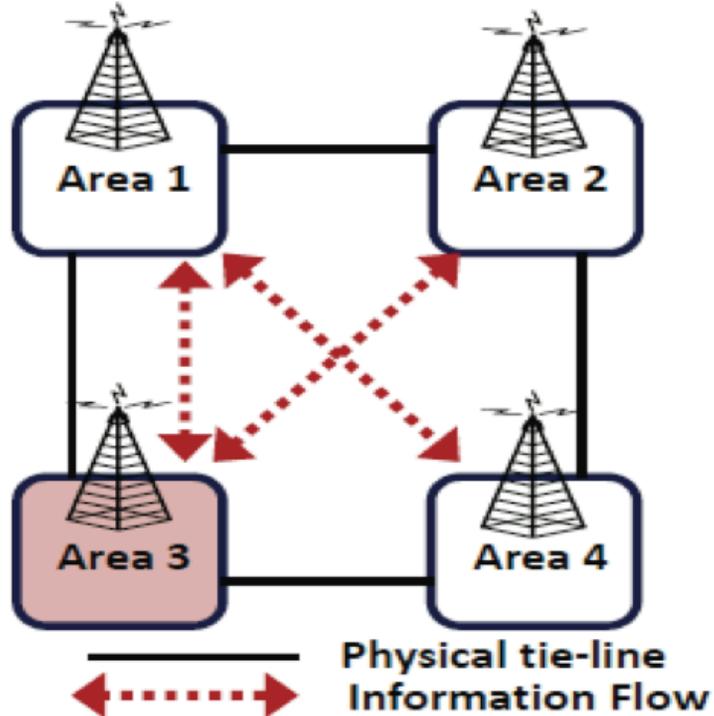
Motivation

- Computational & communications challenge:
 - **fast sensing** (e.g., Phasor Measurement Units) produces big data, and communications bottlenecks
- Restructuring/deregulation means more RTOs, or **control areas** (CAs)
- **Situational awareness** needed for large interconnected power systems:
 - wide area monitoring, control and protection (WAMCP)
- Of interest: a **distributed estimation** framework to obtain the **system-wide states** through information exchange among CAs.

Proposed Solution

Wide area state estimation via distributed iterative information processing:

Conceptual Model



Key Properties

- No central coordinator
- Only **local information** (measurement Jacobian matrix, measurement vector) required
- All local control areas **not necessarily observable**
- Flexible in communication topology
- **Equivalent** performance to **centralized** approach

Distributed Algorithms for State Estimation



Distributed Measurement Model

- System State

- $\theta \in \mathbb{R}^M$: The network system state (vector) consisting of voltage phase angles of buses in all CAs.

- CA Local Observation Model

- $\mathbf{z}_n \in \mathbb{R}^{M_n}$: The local observation at CA n

$$\mathbf{z}_n = H_n \theta + \mathbf{e}_n,$$

where the Jacobian $H_n \in \mathbb{R}^{M_n}$ sub-block represents the local physical interconnections.

Proposed Distributed Iterative Solution

[w / Xie, Choi, Kar - T-SG'12]

Each CA n has only local knowledge of the network structure and measurements and updates a local estimate \mathbf{x}_n as follows:

$$\mathbf{x}_n(t+1) = \mathbf{x}_n(t) - \beta_t \sum_{l \in \Omega_n} (\mathbf{x}_n(t) - \mathbf{x}_l(t)) + \alpha_t \bar{H}_n^T (\bar{\mathbf{z}}_n - \bar{H}_n \mathbf{x}_n(t)),$$

where

- Ω_n : communication neighborhood of CA n
- $\bar{H}_n = R_n^{-1/2} H_n$
- $\bar{\mathbf{z}}_n = R_n^{-1/2} \mathbf{z}_n$



Convergence to Global Estimates

[w / Xie, Choi, Kar - T-SG'12]

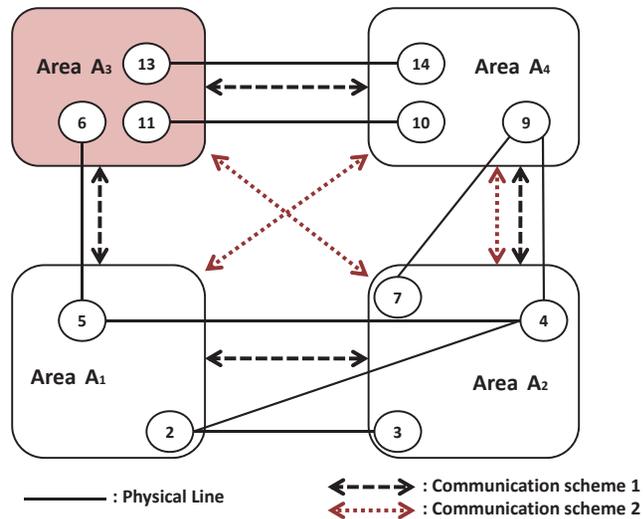
Global observability of the grid (i.e., $\sum_{n=1}^N H_n^T H_n$ is full rank)

+ connectivity of the communication network (i.e. the second smallest eigenvalue of the graph Laplacian is positive) ...

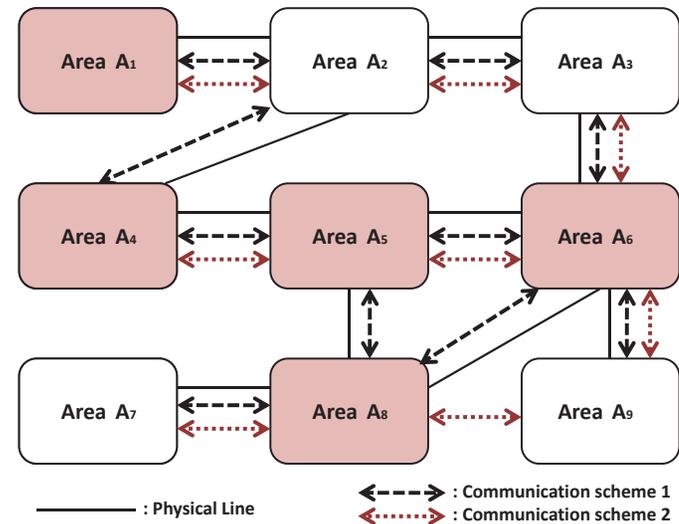
assures a.s. convergence of local estimates to the global estimate (least squares with all measurements) with appropriately programmed α 's and β 's.



Test Bus Systems



(a) The IEEE 14-bus system



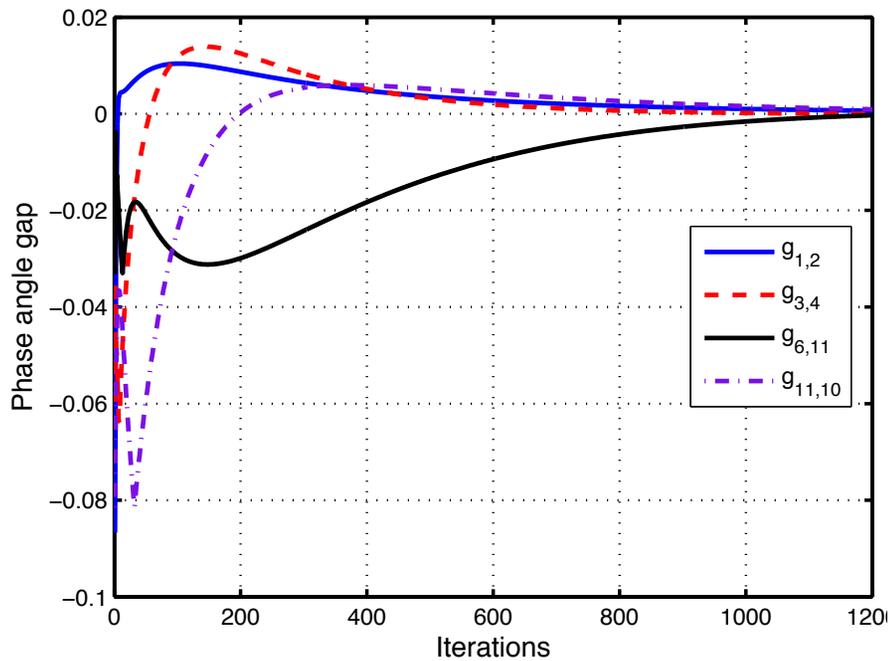
(b) The IEEE 118-bus system

- Overall systems are globally observable
- CAs are globally unobservable
- Shaded CAs are locally unobservable

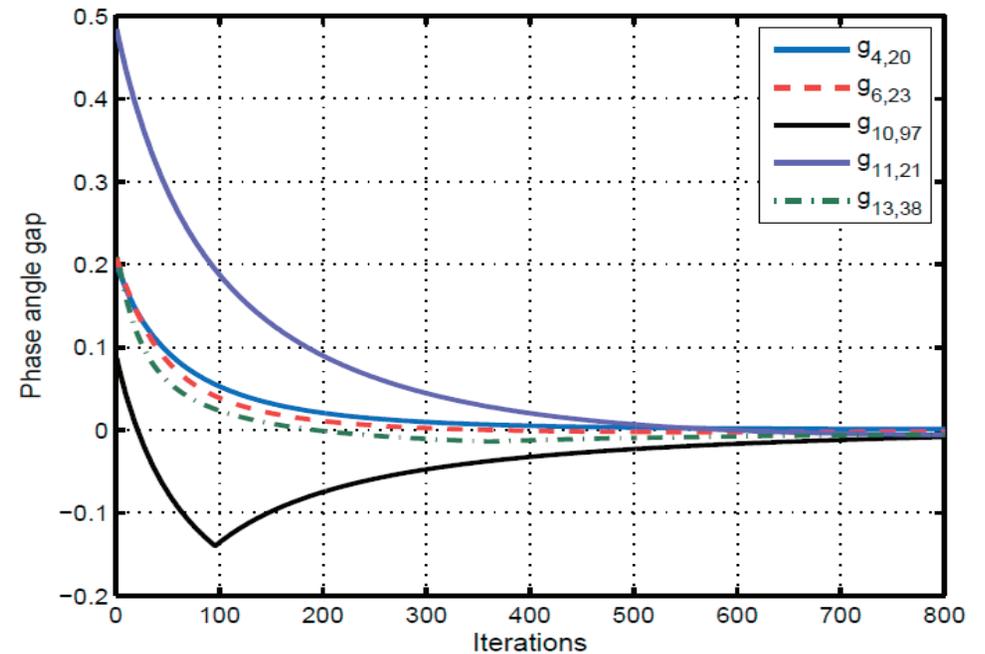
Distributed Algorithms for State Estimation



Convergence of Phase Estimates



14-Bus System

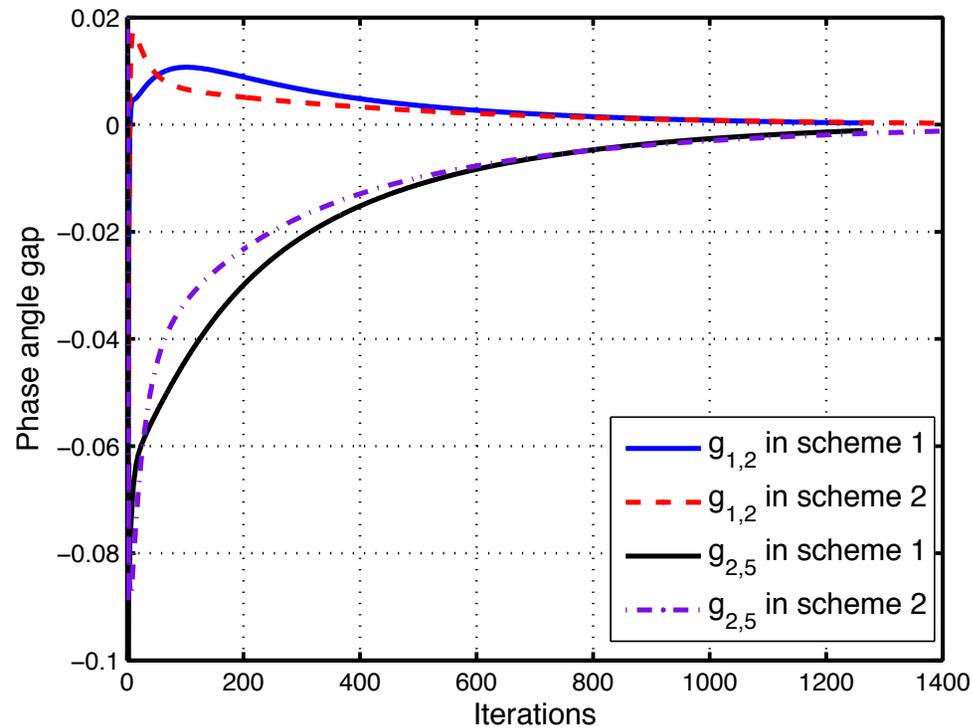


118-Bus System

Distributed Algorithms for State Estimation



Communication Topology Flexibility



14-Bus System

Distributed Algorithms for State Estimation



Related Work

- **Nonlinear** (AC) state estimation [w/ Xie, Choi, Kar, T-SG'12]
- **Multi-cast routing** [w/ Li, Lai, JSAC:SG Series'12]
- **Games** for **privacy**-aware **distributed** state estimation [w/ Belmega, Sankar – NetGCoop'12 & T-SG (submitted)]

Distributed Algorithms for State Estimation



Summary

Three Topics in Smart Grid:

- *Game Theoretic Methods* for Modeling Interactions
- *Privacy-Utility Tradeoffs* for Data Sources
- *Distributed Algorithms* for State Estimation

Games, Privacy and Distributed Inference for the Smart Grid



The background of the slide is a solid dark blue color. Overlaid on this background are several overlapping, wavy white lines that create a sense of depth and movement, resembling a stylized landscape or a series of ripples. The lines are more prominent in the upper and right portions of the slide.

Thank You!